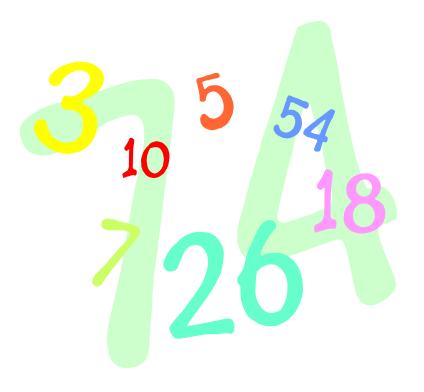
Adopted: December 2019 Approved by the Headteacher Next Review Date: December 2021 Owner: Maths Subject Leader



St Paul's C of E Junior School Oxford Road, Wokingham, Berkshire, RG41 2YJ T 0118 9785219 E <u>admin@stpauls.wokingham.sch.uk</u> W <u>www.stpauls.wokingham.sch.uk</u>

Calculation Policy

Adapted, with permission, from NJC Education Consultancy Ltd. Draft Calculation Policy



Introduction:

Children are introduced to the processes of calculation through practical, oral and mental activities. As they begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, so that they develop both **conceptual understanding** and **fluency** in the fundamentals of mathematics. Whilst interpreting signs and symbols involved with calculation, orally in the first instance, children use both manipulatives as well as pictorial representations (potentially as part of a **Concrete-Pictorial-Abstract – CPA – approach**) to support their mental and written methods of calculation. As children's mental methods are strengthened and refined, they begin to work more efficiently, which will support them with using succinct written calculation strategies as they are developed.

From Early Years to Year 1:

There are fundamental concepts that it is important for children to develop an early understanding of as building blocks to future learning in maths, including that linked to calculation. A selection of the skills include:

- Ordinality 'the ordering of numbers in relation to one another' e.g. (1, 2, 3, 4, 5...)
- Cardinality 'understanding the value of different numbers' e.g. (7 = 2000 17 = 2000 + 2000 14 =
- Equality 'seven is the same total as four add three' e.g.
- Subitising 'instantly recognising the number of objects in a small group, without counting them' e.g.
 - \rightarrow five

- One-to-one correspondence e.g.
- Conservation of number 'recognising that a value of objects are the same, even if they are laid out differently' e.g.



- Concept of zero
- 3 + 0 = 3
- Counting on and back from any number e.g. 'five add three more totals eight'



'ten take away three totals seven'

The ability to calculate mentally forms the basis of all methods of calculation and has to be maintained. In the 2018 national Key Stage 1 SATs tests, every one of the named mental maths strategies below was assessed, whilst many also featured in a less explicit manner in the Key Stage 2 SATs tests, hence highlighting the need for each method to be taught explicitly. A good knowledge and 'feel' for numbers, is the product of structured practice through progression in relevant practical maths experiences alongside visual representations.

By the end of Year 6, children should be equipped with efficient mental and written calculation methods, which they use fluently. Decisions about when to progress should always be based on the security of pupils' understanding and their readiness to move ahead to the next stage. At whatever stage in their learning, and with whatever written method is being used, children's strategies must still be underpinned by a secure understanding and knowledge of number facts that can be recalled fluently with flexibility.

The overall aims are that when children leave primary school they:

- Are able to recall number facts with fluency, having developed conceptual understanding through being able to visualise key ideas such as those related to place value, through experience with practical equipment and visual representations;
- Make use of diagrams (including the bar model) and jottings to help record / reason through stages of thinking when using mental methods that generate more information than can be kept in their heads;
- Have an efficient, reliable, written method of calculation for each number operation that they can apply with confidence when undertaking calculations that they cannot carry out mentally;
- Are able to make connections between all four number operations, understanding how they relate to one another, as well as how the rules and laws of arithmetic can be applied.

Disclaimer:

The NCETM, 2015, state that, 'A pupil really understands a mathematical concept, idea or technique if he or she can represent it in a variety of ways,' and this calculation policy aims to show multiple representations of concepts as often as possible. It is intended that both addition/subtraction and also multiplication/division are taught with an **interconnectedness**, as opposed to in isolation.

This policy has been adopted from a draft policy produced by the independent maths consultant, Nathan Crook, with whom we have been working alongside to develop our curriculum planning and subject specific teaching skills. It encompasses statutory requirements as detailed in the National Curriculum (2014) and has a correlation to year-by-year expectations set out in the programmes of study for mathematics.

Addition:

Mental calculation strategies for addition and subtraction:

All mental calculation strategies need to be taught explicitly using a Concrete – Pictorial – Abstract (CPA) approach in every year group, for example, using decimals in Key Stage 2. The following ideas can be adjusted so that they are accessible to all children. The NCETM, 2015, state that, 'a pupil really understands a mathematical concept, idea or technique if he or she can represent it in a variety of ways.'

Doubles: 8 + 8 = 16	Near doubles: 6 + 7 = 13	Number bonds: 7 + 3 = 10
8 + 8 is connected to 8 X 2	6 + 7 is commutative with 7 + 6	
Partitioning: 14 + 12 = 26	Bridging: 7 + 5 = 12	Adjusting: 16 + 9 = 25
	To begin: 7 + 3 = 10 Then: 10 + 2 = 12	To begin: 16 + 10 = 26 Then: 26 – 1 = 25
		1234567891011121314151617181920212223242526272829303132333435363738394041424344454647484950

	Finding the difference: $10 - 6 = 4$		e.g. ca order To beg Then: 7	ering: $8 + 7 + 2 = 17$ lculating numbers in a different in: $8 + 2 = 10$ 10 + 7 = 17	
	Counting	Mental maths strategies & linked concepts	Rapid recall		models/images to support conceptual rstanding
Stage 1:	Count in ones to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.	Explicitly teach every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction. - 3 + - 2	Rapid recall of all pairs of numbers totalling numbers up to 20. Use structured apparatus – i.e. Numicon, tens frames, abaci, etc.	 Combining two groups: Teachers model how to line up counters/objects on a number track before counting on. This is a precursor to use of a fully numbered number-line. Children develop a mental picture of the number system for use with calculation. A range of key models and images support this, alongside practical equipment. 	0230567890 3+2=5 'Three plus two is the same as five' 'Eight add two more makes ten' 'Eight add two more makes ten'
				 Whole / part-whole model: The concept of a whole / part- whole model is introduced. 	Image: second

		'Four add one is the same as five'			Cherry model
Stage 2:	Continue practising above skills. Count in steps of 2, 3 and 5 forwards and backwards to and from zero using a counting stick set up as a number line. Count in tens from any number – link to coins in a piggy bank as well as a number square.	Explicitly teach every mental maths strategy detailed above. Round numbers to the nearest 10, for example, by illustrating on a number line that is drawn on a folded strip of paper.	Recall addition facts for all numbers to 20.	 Counting on from the largest number: Children begin to use number lines to support their own calculations, initially counting on from the largest number in ones before beginning to work more efficiently. Reordering calculations to apply use of mental maths strategies: Children reorder 'strings' of numbers to apply their understanding of mental maths strategies, including doubles and number bonds, e.g. 6 + 7 + 4 reordered to 6 + 4 = 10 and then 10 + 7 = 17. Jottings are used to help keep track of thinking. Whole / part-whole model: 	Number line with all numbers labelled 0 1 2 3 4 5 6 7 8 9 10 11 12 18 + 5 +1 +1 +1 +1 +1 18 +9 20 21 22 23 24 18 19 20 21 22 23 Questions such as: 'How might I rearrange these to find the total?' are asked.
				 The concept of a whole / part- whole model is reinforced and extended. 	Bar model

Stage 3:	Continue practising above skills. Count forward and backwards from 0 in multiples of 4, 8, 50 and 100. Count on 10 or 100 from any two- digit number. Count up and down in tenths. Link to a counting stick as before, whilst deriving number facts.	Reinforce partitioning and bridging through multiples of 10, plus adjusting when adding 11 or 9. Use structured apparatus to understand that subtraction undoes addition and link with inverse number operations.	Connect pairs totalling ten to pairs of multiples of 10 totalling 100. Use 10ps in tens frame. Recall pairs of two-digit numbers with a total of 100, i.e. 32 + ? = 100.	 Expanded horizontal addition: Teachers model how numbers can be partitioned into tens and ones, including different ways, e.g. 36 = 30 + 6 36 = 20 + 10 + 6 Add numbers using structured apparatus to support understanding of place value. Make connections between partitioning both numbers using structured apparatus and partition the second number only using a number line. 	= Add
Stage 4:	Continue practising previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and	Bridging through 60 for time, i.e. 70 minutes = 1 hour and 10 minutes. Rounding any number to the	As above. Use known facts and place value to derive new ones, i.e. 'If I know 8 + 3 = 11, I also know	 Expanded horizontal method, leading to columnar addition: Written recording should follow teacher modelling around the size of numbers and place value using a variety of concrete/pictorial materials, e.g. Numicon shapes, Dienes and place-value cards. 	

1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, hundredths and simple fractions using models and images, plus Dienes / pixie Dienes equipment and a counting stick.	nearest 10, 100 or 1000. Rounding numbers with one decimal place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of answers.	0.8 + 0.3 = 1.1 and 8/100 + 3/100 = 11/100.' Sums and differences of pairs of multiples of 10, 100 or 1000. Addition doubles of numbers to 100. Pairs of fractions totalling one.	 As children move towards using a columnar method, links continue to be made with earlier models and images, including the number line. 	
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Stage 5:	Count forwards and backwards in steps of powers of 10 for any given number up to one million. Continue to count forwards and backwards in simple fractions. Count forward	Use apparatus and knowledge of place value to add decimals, i.e. 3.4 + 2.5 = 5 + 0.9 Reorder increasingly complex calculations, i.e. 1.7 + 2.8 + 0.3 = 1.7 + 0.3 + 2.8	Continue to practice previous stage and make links between known facts and addition pairs for fractions, percentages and decimals Doubles and halves of	 Expanded vertical method, leading to columnar addition: Teachers model a column method that records and explains partial mental methods. There remains an emphasis on the language of calculation, e.g. 'Forty plus seventy equals one-hundred and ten.' 'Seven add six equals thirteen.'before recombining numbers. Teachers also model the language of: 'Four tens add seven tens total eleven tens or 	Informal columnar: Adding the hundreds first: 471 +356 700 120 -7 827 Adding the ones first: 471 +356 7 120 -7 827 Adding the ones first: 471
	and backwards in appropriate decimals and percentages.	Compensating – i.e. 405 + 399 → add 400 and then subtract one.	decimals, i.e. half of 5.6, double 3.4. Sums and differences of decimals, i.e. 6.5 + 2.7	 Teachers similarly advance to model the addition of two 3- digit numbers with the expectation that as children's knowledge of place value is secured, they become ready to approach a formal compact method. 	

Stage 6:	Continue to practice previous skills. Count forwards and backwards in simple fractions, decimals and percentages.	Bridging through decimals, i.e. 0.8 + 0.35 = 0.8 + 0.2 + 0.15 using empty number lines. Partitioning using near doubles, i.e. 2.5 + 2.6 = 5 + 0.1 Reorder decimals, i.e. 4.7 + 5.6 - 0.7 as $4.7 - 0.7 + 5.6 = 4 + 100$	Using children's confident recalling of basic facts to 20/100 and deriving facts using place value, make links between decimals, fractions and percentages. i.e. 1 + 19 10 + 190	 Columnar addition (formal written method): The concept of exchange is reinforced through continued use of manipulatives. Teachers model: "I have two tens and five ones, which need adding to four tens and seven ones." "I add five ones to seven ones, which gives me twelve ones." "I exchange ten of my twelve ones for a ten counter." "I add my three tens and 	Pupils to be encouraged to consider mental strategies first.Formal columnar – using an example with smaller value numbers to exemplify: 25 ± 47 -2 25 ± 47 -1 TensTensOnesTens 0
		5.6. 100 + 1900 Question: What do you notice?	four tens to make seven tens." "Altogether, I have seven tens and two ones." • Teachers similarly advance to model the addition of two 3- digit numbers and then go beyond. 587 <u>+ 475</u> <u>1062</u> 1 1	$\begin{array}{c} 25 \\ +47 \\ \underline{2} \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ $	

Subtraction:

	Counting	Mental strategies	Rapid Recall	Written calculation and conceptual understand	d appropriate models and images to support ding
Stage 1:	Count in ones to and across 100, forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten.	Explicitly teach every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction: -3 $+$ -2	Rapid recall of subtraction facts for numbers up to 10. Use structured apparatus, i.e. Numicon, tens frames, abaci etc.	Subtraction as taking away from a group: • Teachers model how to remove counters/objects and count back on a number track. This is a precursor to use of a fully numbered number-line.	'Five minus two totals three' 'Six take away two leaves four' 'One less than six is five'
		'One less than five is four'		 Whole / part-whole model: The concept of a whole / part-whole model is introduced. 	Tens frame Bar model
Stage 2:	Continue practising above skills. Count in steps of 2, 3	Explicitly teach every mental maths strategy detailed above.	Recall subtraction (and addition) facts for all	 Taking away: Children begin to use number lines to support their own 	Number line with all numbers labelled 0 1 2 3 4 5 6 7 8 9 10 11 12

	and 5, forwards and backwards to and from zero. Count in tens from any number –		numbers to 20.	calculations, initially counting back in ones before beginning to work more efficiently.	13-5=8 $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$ $13-5=8$
	link to coins in a piggy bank as well as a number square.			Finding the difference: • Teachers model how to find the difference when two numbers are relatively 'close together.'	Comparing two sets to find the difference.
Stage 3:	Continue practising above skills. Count from 0 in multiples of 4, 8, 50 and 100. Count on and back by 10 or 100 from any two digit number. Link to counting stick counting forwards and backwards flexibly.	Reinforce partitioning and bridging through multiples of 10, plus adjusting when subtracting 11 or 9. Use structured apparatus to understand that subtraction undoes addition and link with inverse number operations.	Connect subtractions from ten to subtractions from multiples of 10 totalling 100. Use 10ps in tens frame. Subtract two digit numbers	 When teaching children about reduction, highlight the importance of only partitioning one number. 	Subtraction by partitioning with use of manipulatives and linked with a horizontal expanded written algorithm: 167 - 24 = 143 20 4 In either order To begin: $167 - 20 = 147$ Then: $147 - 4 = 143$

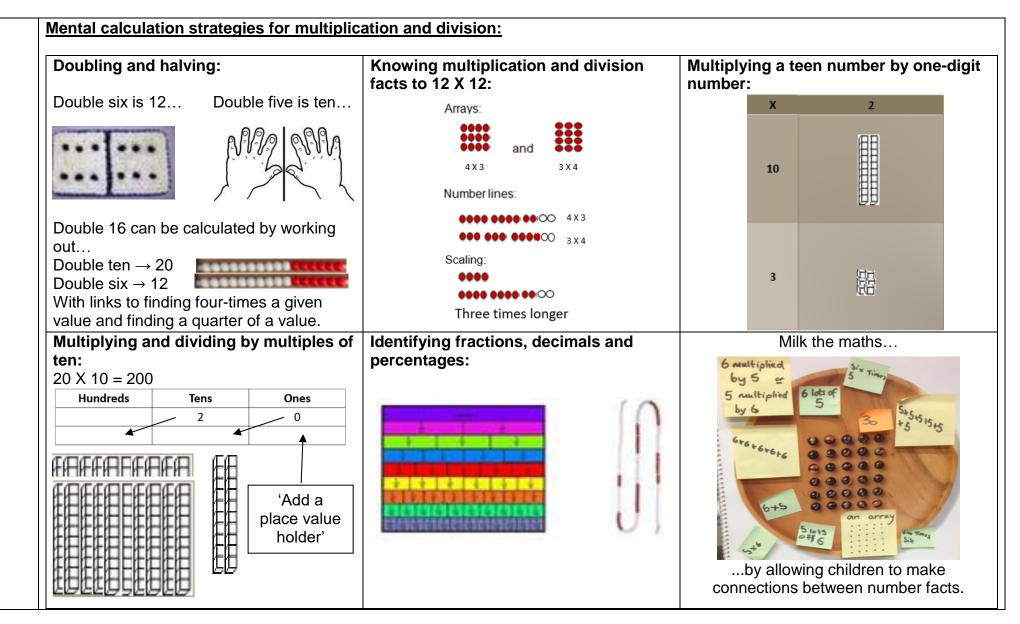
	Count up and down in tenths – linking to visual image.		from 100 i.e. ? = 100 - 78	Finding the difference: • Children move on to find the difference by making number line comparisons.	100 + 60 + 7 $- 20 + 4$ $0 + 40 + 3$ Finding the difference on a number line: $100 + 60 + 7$ $- 20 + 4$ $- 20 + 4$ $- 20 + 40 + 3$ Finding the difference is $100 + 60 + 7$ $- 20 + 40$ Finding the difference is $- 20 + 40$ $- 20 + 40$ Finding the difference is $- 20 + 40$ Finding the difference
Stage 4:	Continue practising of previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and 1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, hundredths	Bridging through 60 for time, i.e. 70 minutes = 1 hour and 10 minutes Rounding any number to the nearest 10, 100 or 1000. Rounding numbers with one decimal place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of answers.	As above. Use known facts and place value to derive new ones, i.e. 'If I know 11 - 3 = 8, I also know 1.1 - 0.3 = 0.8 and 8/100 - 3/100 = 5/100.' Sums and differences of pairs of multiples of 10, 100 or 1000.	 Subtraction by partitioning with use of manipulatives, and including transfer / exchange, linked with a horizontal expanded written algorithm in preparation for a future formal column method. 	363 - 147 = 216 50 13 300 + 60 + 3 -100 + 40 + 7 200 + 10 + 6 a a b

	and simple fractions using models and images, i.e. Dienes / Pixie Dienes equipment, counting stick, ITPs.	Subtraction of fractions totalling 1, i.e. $1 - 0.3 =$ 0.7		
			Finding the difference: • Finding the difference continues to be highlighted where the two numbers are close together – using a number line on a strip of paper.	0
Stage 5:	Count forwards and backwards in steps of powers of 10 for any given number up to one million. Continue to count forwards and backwards in simple	Continue to practise previous stage and make links between known facts and addition pairs for fractions, percentages and decimals.	Column method with Dienes: • Subtraction by partitioning with use of manipulatives, and including transfer / exchange, linked with a formal column written algorithm.	51 363 -147 216

	fractions. Count forward and backwards in appropriate decimals and percentages.	subtract 400 and then add 1.	Doubles and halves of decimals, i.e. half of 5.6, double 3.4. Sums and differences of decimals, i.e. 6.5 + 2.7		
Stage 6:	Continue to practise previous skills. Count forwards and backwards in simple fractions, decimals and percentages.	Bridging through decimals, i.e. 1.5 – 0.8 = 1.5 – 0.5 then – 0.3 using empty number line.	Using children's confident recalling of basic facts to 20/100 and using place value, make links between decimals, fractions and percentages. 19 - 1 = 190 - 10 = 1900 - 100 = 1.9 - 0.1 = Question: What do you notice?	 Column method with place value counters: The concept of transfer / exchange is continued through use of manipulatives. Teachers model: "I have seven tens and two ones. I need to subtract four tens and seven ones." "At the moment, I cannot subtract seven ones from two ones, so I need to 	Pupils to be encouraged to consider mental strategies first. Formal columnar – using an example with smaller value numbers to exemplify: $\begin{array}{c}72\\-47\\\hline \hline 800\\\hline 000\\\hline $

transfer one
ten to
become ten
ones."
3. "Now I can
take away
seven ones
from twelve
ones, so that
I have fives
ones left."
4. "I can now
subtract four
tens from six
tens, which
leaves me
with two
tens."
5. "I recombine
two tens and
fives ones to
understand
that I am left
with twenty-
five."

Multiplication:



	Counting	Mental strategies	Rapid recall	Written calculation a support conceptual	and appropriate models and images to
Stage 1:	Count forwards and backwards in 2s, 5s and 10s	Doubling up to six and then ten whilst using related models and images.	Derive/recall doubles up to five and derive/recall halves up to ten.	Developing early conceptual understanding of multiplication (grouping):	Use objects, pictorial representations and arrays to show the concept of multiplication:
Stage 2:	Count forwards and backwards in 2s, 3s, 5s and 10s from zero.	Begin to understand and use inverse number operations: 10 2 5 Stories are used alongside a triad to help children understand links between number operations, e.g. "There are five pencils in two packs, which means that there are ten pencils altogether." Doubling is reinforced using a whole/part-whole model:	Derive/recall doubles up to ten and derive/recall halves up to twenty. Recall & use multiplication facts for the 2X, 5X and 10X-tables. Learn what happens when a number is multiplied by zero or one.	Understanding multiplication as repeated addition: Investigate multiplication as repeated addition, so that the law of cummutativity is understood. Whilst arrays are also modelled explicitly at this stage, it is important to note that they will continue to	Arrays: 5×3 3×5 3×6 3×6 3×10^{10} repeated addition images. Repeated addition on the number line linked with manipulatives: $6 \times 4 = 24$ 5×6 6×6

Stage 3:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero. Count up and down in tenths.	Use doubling to make connections between the 2X, 4X and 8X-tables. Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4 Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon $\sum_{2cm} \underbrace{5cm}_{8cm}$	Recall and use multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	be a key model at later stages, alongside more formal methods of calculation. Relate multiplying a 2-digit by 1-digit number using repeated addition and arrays to represent:	$ \begin{array}{c} $	X 10 = 40 $20 24 28 32$ 10 3 20 2 21	4 X 2 = 8 36 40 44 48 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Stage 4:	Counting forwards and backwards	Derive factor pairs of numbers using models and images, e.g. Cuisenaire 1 and 12	Recall & use multiplication facts for all times-tables	Relate multiplying a 3 or 2-digit by 1- digit number with arrays towards	Relate multiply whilst refining t		y 1-digit number, tion used.

	in 2s, 3s, 4s, 5s, 7s,	2 and 6 3 and 4	up to 12 X 12.	using long/short multiplication:	114 X 2 = 228		
	8s, 10s,		12.		X 100	10	4
	25s and 1000s from zero. Count up and down in tenths				2		
	and						
	hundredths.	Use reordering to multiply three numbers.			114 X 2 =		
		Children learn about the associative law: (9 X 5) X 10 = (10 X 5) X 9			$ \begin{array}{c} 100 X 2 = 200 \\ 10 X 2 = 20 \\ \underline{4 X 2 = 8} \\ $	Link with distrib (100 X 2) + (1 (4 X 2) = 1	0 X 2) +
					At this stage, the ne the National Curricu short multiplication; an expanded form above) is be a bette multiplication.	ulum suggests however, the t of calculation (a	teaching eam feel that as set out
Stage 5:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 4/3/2-digit by 1/2- digit number with grid to using long multiplication:	10	10 8 100 80 30 24 18 24 30 24 30 80 100 234	

Stage 6:	Consolidate all previous counting, including forwards and backwards in fractions.	Perform mental calculations, including with mixed numbers and operations.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 4/3/2-digit by 1/2- digit number with grid to using short multiplication:	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
					Once children have fully grasped the concept of multiplication alongside manipulatives and an expanded written method, they will be well- placed to progress towards a more compact written algorithm.

Division:

	Counting	Mental strategies	Rapid recall	Written calculation a support conceptual	and appropriate models and images to understanding
Stage 1:	Count forwards and backwards in 2s, 5s and 10s	Doubling up to six and then ten whilst using related models and images.	Derive/recall doubles up to five and derive/recall halves up to ten.	Developing early conceptual understanding of division as grouping and sharing:	Use objects, pictorial representations and arrays to show the concept of division as grouping and sharing.
Stage 2:	Count forwards and backwards in 2s, 3s, 5s and 10s from zero.	Begin to understand and use inverse number operations.	Derive/recall doubles up to ten and derive/recall halves up to twenty. Recall and use multiplication	Understanding division as repeated subtraction: • Investigate division as repeated subtraction. • Through teacher	Number lines: $12 \div 3 = 4$ $12 \div 3 = 4$ 3 = 3 3 =

		Stories are used alongside a triad to help children understand links between number operations, e.g. "15 children are asked to get into three groups and find out that there are five people in each group."	facts for the 2X, 5X and 10X-tables.	modelling, children need to know that division is not commutative.	$15 \div 5 = 3$ $0 \qquad 5 \qquad 10 \qquad 15$ Early bar model
Stage 3:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero.	Use doubling to make connections between the 2X, 4X and 8X-tables. Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4 Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon.	Recall & use multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	Dividing a 2-digit by 1-digit number, representing this efficiently on a number line:	Children use an empty number line to chunk efficiently. $96 \div 6 = 16$ $6 \times 6 = 36$ $10 \times 6 = 60$ 4 0 36 $96Conceptual understanding can be providedthrough use of a bead string to highlight thechunks.$
Stage 4:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 7s, 8s, 10s, 25s and 1000s from zero.	Derive factor pairs of numbers using models and images, e.g. Cuisenaire.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Dividing a 3 or 2- digit by 1-digit number, representing this efficiently on a number line, also in relation to long division: • At this stage, remainders may be	Children use an empty number line to chunk efficiently. $224 \div 8 = 28$ $8 \times 8 = 64$ $20 \times 8 = 160$ 0 64 224

Stage 5: Stage	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	Recall & use multiplication facts for all times-tables up to 12 X 12.	present in a practical context. Dividing a 4/3/2- digit by 1-digit number, in relation to long division: • By this stage, there is a statutory requirement that children can use a formal written calculation method, such as long division. • Short division may begin to be taught alongside long division, but still with use of visual representations Dividing a 4/3/2-	28288224-160 (8×20) 64or64 (8×8) 0 0 As schools have autonomy to decide children's progression in learning between long and short division in Years 5 and 6, the maths team suggest beginning with long division.Remainders should be interpreted in the following ways when long division is used:• as whole numbers• as fractions• through rounding in an appropriate way to the contextLong division:415 ÷ 9 = 46 and 1/9946 and 1/9941540 X 9 = 360556 X 9 = 541
6:	all previous counting, including forwards and	including with mixed numbers and different number operations.	multiplication facts for all times-tables up to 12 X 12.	digit by 2/1-digit number, in relation to long and then short division:	progression in learning between long and short division in Years 5 and 6, the maths team suggest moving from long division to short division.

backwards in fractions.	 calcula method includii and sh division Use of represe – like ti 	s afollowing wayry•throughry•througheto the ofildrenLong division:e432 \div 15 = 28written432 \div 15 = 28ation20 X 15 = 30ort13n.20 X 15 = 30ort13n.8 X 15 = 12visual $\frac{12}{15} = \frac{4}{5}$ ppositeAnswer: 28 $\frac{4}{5}$ ant.Short division:	when she rounding context 4/5 8 2 0 2 0 2	ort division	
		138 ÷ 6 = 23	Hundreds	Tens	Ones
		6 \1 ² 3 8			
		6	23 • • • • • • • • • • • • • • • • • • •		23

	Key language:
	'How many groups of six one-hundreds are
	there in one-hundred?'
	'How many groups of six tens are there in
	thirteen tens?'
	'How many groups of six ones are there in
	eighteen?'